



# Rollover Prevention Using Active Suspension System

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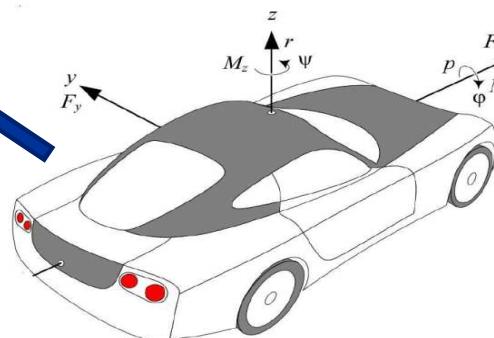
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# Context: SYSCOVI project of the region Hauts-de-France

System of Systems approach for the COntrol of the dynamics of Intelligent Vehicles

*UTC – HeuDiaSyC*

*R. Talj*



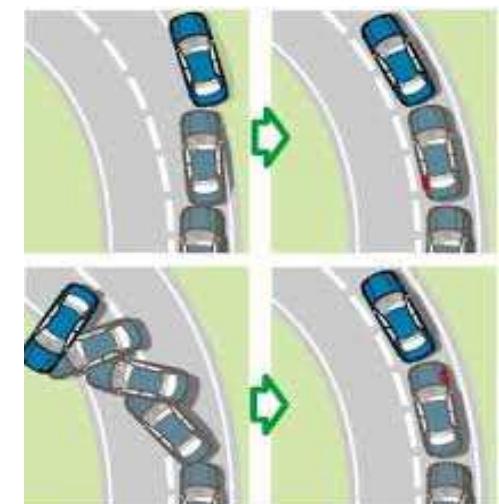
*UPJV – MIS*

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Several stabilization systems exist:

**DYC (“Direct Yaw Control”), Active Steering (AS),  
(semi-)active suspensions**

**Each system has its own limitations with respect to the driving conditions.**

## Objectives

Global Chassis Control (GCC) reliable, comfortable, and robust

- Development of control architectures (decentralized or hierarchical) to ensure the cooperation of the actuators in the System of Systems (SoS).
- **Fault tolerant control** of the over-actuated system, for an improved reliability.
- Study of the technology of **In-wheel Electric Vehicles (IEV)**, and consideration of the energy consumption.

Experimental evaluation of the results on real data acquired on the platforms of the Equipex Robotex project in Heudiasyc laboratory.

# Plan

- 1. Motivation**
- 2. Rollover problem formulation**
  - Rollover dynamics
  - Rollover avoidance possible solutions
- 3. Contribution**
  - Vehicle Dynamics
  - Active Suspensions control for rollover prevention
- 4. Conclusion and perspectives**

# Motivation

- 90% accidents

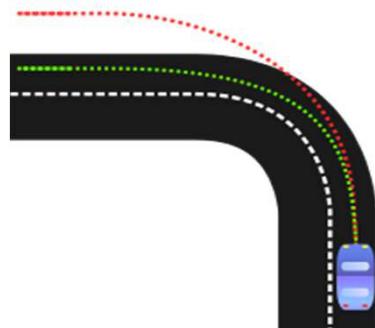


human errors

Lateral skidding



Understeer



Rollover



# Motivation

- Vehicle rollover constitutes **ONLY 3%** of all accidents !!

But it causes:

- Fatal injuries, nearly **33% of all deaths** from passenger vehicle crashes (NHTSA, 2011)



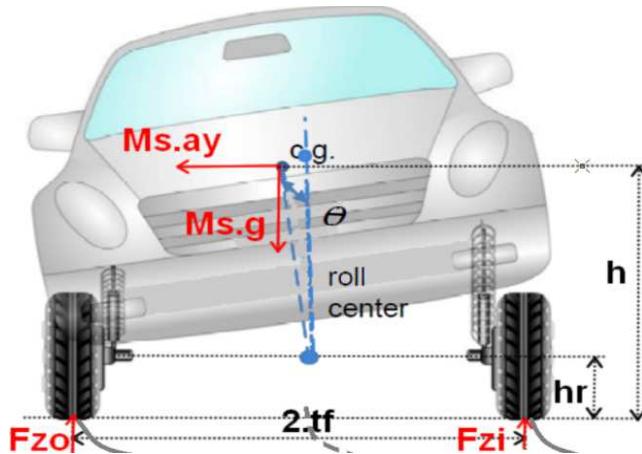
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# Rollover problem formulation

When cornering:

- The lateral acceleration induces a roll angle towards the outside of the corner.
- A vertical load transfer occurs toward the outside.
- The outside wheels vertical forces  $F_{z_o}$  increase, and the inside wheels vertical forces  $F_{z_i}$  decrease.



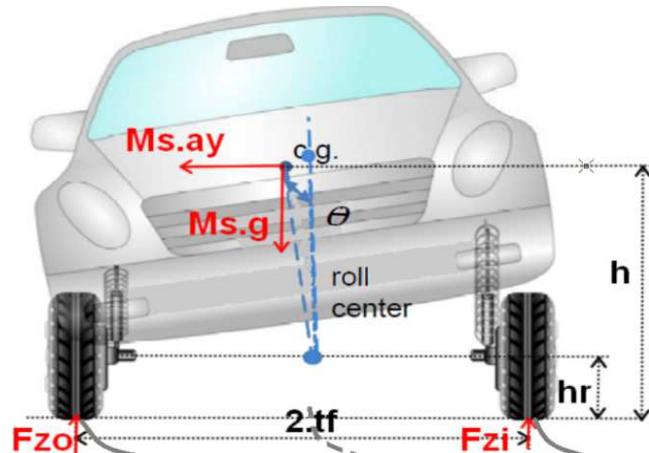
**Equation of motion around outside wheels axis:**

$$M_s \cdot a_y \cdot h - M_s \cdot g \cdot (t_f - (h - hr) \sin \theta) + F_{zi} \cdot 2 \cdot t_f = 0$$

**Rollover starts when  $F_{zi}$  become 0**

$$a_{y\_lift\_off} = \frac{t_f - (h - hr) \cdot \theta}{h} g$$

# Rollover problem formulation



- Equation of motion around outside wheels axis:

$$M_s \cdot a_y \cdot h - M_s \cdot g \cdot (t_f - (h - hr) \sin \theta) + F_{z_i} \cdot 2 \cdot t_f = 0$$

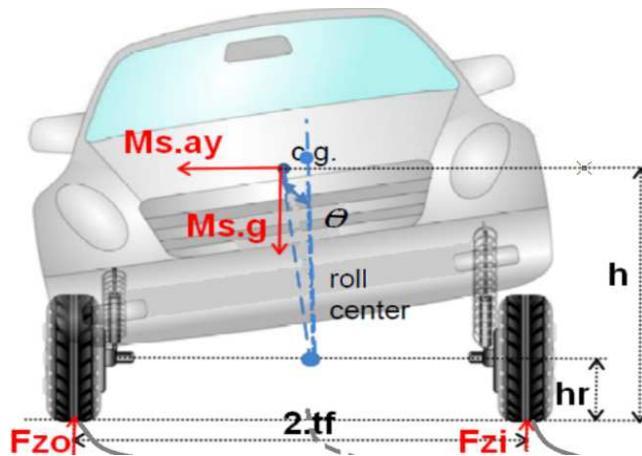
- Rollover starts when  $F_{z_i}$  become 0

$$a_{y\_lift\_off} = \frac{t_f - (h - hr) \cdot \theta}{h} g$$

$$a_{y\_safe} = 0.7 a_{y\_lift\_off}$$

- $a_{y\_safe}$  represents the maximal safe lateral acceleration  $a_y$  that the vehicle could handle before starting rollover.

# Rollover avoidance possible solutions



- The vehicle lateral acceleration  $a_y$  should be kept below  $a_{y\_safe}$  to avoid rollover

$$a_y < a_{y\_safe}$$

## Possible actions

Diminish  $a_y$

$$a_y = \frac{V^2}{R}$$

- Braking to diminish  $V$ . (drawbacks on vehicle speed)
- Steering to the outside of the corner to raise  $R$ . (drawbacks on vehicle trajectory)

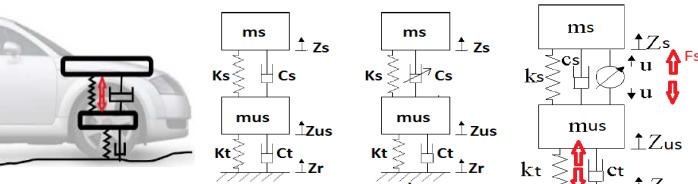
Raise  $a_{y\_safe} = 0.7a_{y\_lift\_off}$

- The vehicle lateral acceleration  $a_y$  should be kept below  $a_{y\_safe}$  to avoid rollover

$$a_y < a_{y\_safe}$$

Possible actions

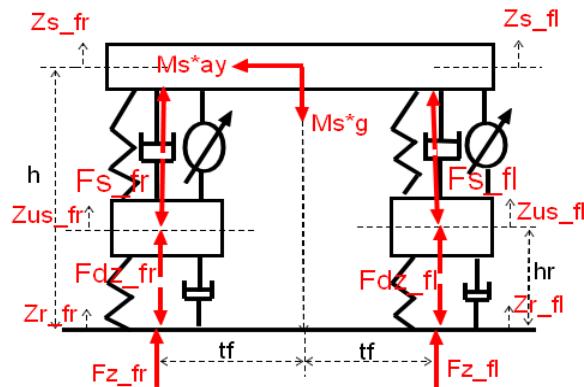
- Semi-active suspensions to diminish  $\theta$  to 0
- Active suspensions to turn the  $\theta$  toward the inside of the corner.



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# Full-vehicle Vertical dynamics



$$F_{s_{ij}} = -k_{s_{ij}}(z_{s_{ij}} - z_{us_{ij}}) - c_{s_{ij}}(\dot{z}_{s_{ij}} - \dot{z}_{us_{ij}}) + U_{ij}$$

$$\ddot{z}_{us_{ij}} = -F_{s_{ij}} + F_{dz_{ij}}$$

$$F_{dz_{ij}} = -k_{t_{ij}}(z_{us_{ij}} - z_{r_{ij}}) - c_{t_{ij}}(\dot{z}_{us_{ij}} - \dot{z}_{r_{ij}})$$

$$\begin{aligned} z_{s_{fr}} &= z - t_f \sin \theta - l_f \sin \varphi \\ z_{s_{fl}} &= z + t_f \sin \theta - l_f \sin \varphi \\ z_{s_{rr}} &= z - t_r \sin \theta + l_r \sin \varphi \\ z_{s_{rl}} &= z + t_r \sin \theta + l_r \sin \varphi \end{aligned}$$

$$F_{z_{ij}} = F_{dz_{ij}} + F_{Z\_LT_{ij}} + m_{ij} \cdot g$$

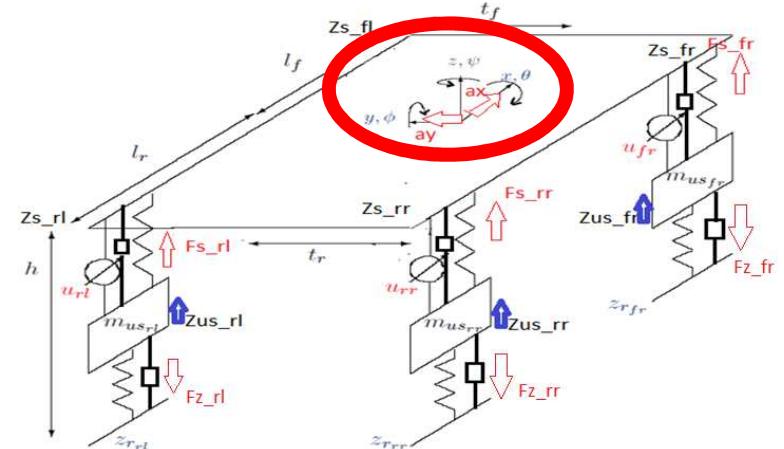
$$F_{Z\_LT_{ij}} = \pm m_{ij} \cdot \left( \frac{h}{tf} \right) \cdot ay.$$

# Full-vehicle Vertical dynamics

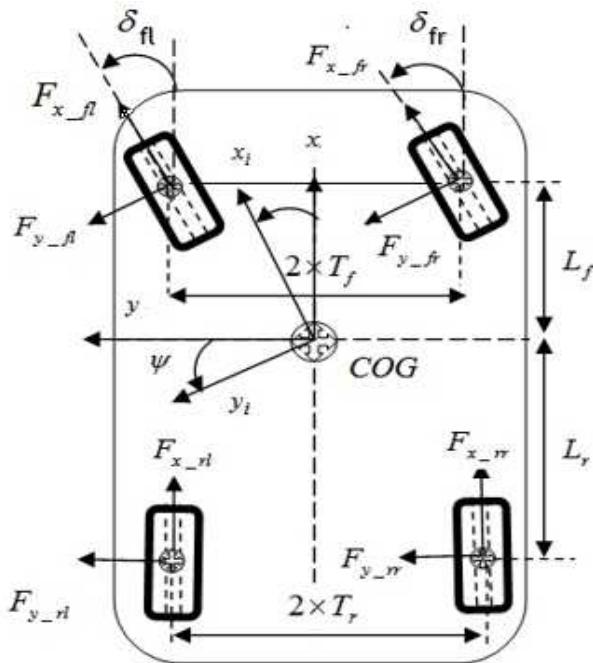
$$\ddot{\theta} = \frac{1}{I_x + M_s h_\theta^2} \left( (-F_{sfr} + F_{sfl}) t_f + (-F_{srr} + F_{srl}) t_r \right. \\ \left. + M_s (h_\theta \cos \theta + z) \cdot a_y + M_s (h_\theta \sin \theta + z) \cdot g \right)$$

$$\ddot{\varphi} = \frac{- (F_{sfr} + F_{sfl}) l_f + (F_{srr} + F_{srl}) l_r \\ + M_s (h_\varphi \cos \varphi + z) \cdot a_x + M_s (h_\varphi \sin \varphi + z) \cdot g}{I_y + M_s h_\varphi^2}$$

$$\ddot{z} = \{F_{sfr} + F_{sfl} + F_{srr} + F_{srl}\} / M_s$$



# Full-vehicle longitudinal / lateral dynamics



$$\ddot{x} = \dot{y}\dot{\Psi} + (F_{x_{fl}} \cos \delta_{fl} + F_{x_{fr}} \cos \delta_{fr} + F_{x_{rl}} + F_{x_{rr}} - F_{y_{fl}} \sin \delta_{fl} - F_{y_{fr}} \sin \delta_{fr})/M$$

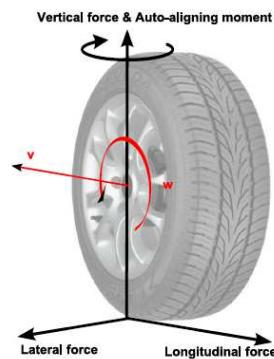
$$a_x = \ddot{x} - \dot{y}\dot{\Psi}$$

$$\ddot{y} = -\dot{x}\dot{\Psi} + (F_{x_{fl}} \sin \delta_{fl} + F_{x_{fr}} \sin \delta_{fr} + F_{y_{rl}} + F_{y_{rr}} + F_{y_{fl}} \cos \delta_{fl} + F_{y_{fr}} \cos \delta_{fr})/M$$

$$a_y = \ddot{y} + \dot{x}\dot{\Psi}$$

$$\begin{aligned} \dot{\Psi} = & \{-t_f(\cos \delta_{fl} F_{x_{fl}} - \cos \delta_{fr} F_{x_{fr}} + \sin \delta_{fr} F_{y_{fr}} - \sin \delta_{fl} F_{y_{fl}}) \\ & + l_f(\sin \delta_{fl} F_{x_{fl}} + \sin \delta_{fr} F_{x_{fr}} + \cos \delta_{fl} F_{y_{fl}} + \cos \delta_{fr} F_{y_{fr}}) \\ & - l_r(F_{y_{rl}} + F_{y_{rr}}) - t_r(F_{x_{rl}} - F_{x_{rr}})\}/I_z \end{aligned}$$

# Tire-road contact (Dugoff model)



$$F_{x_{ij}} = C_\sigma \frac{\sigma_{x_{ij}}}{1 - \sigma_{x_{ij}}} f(\lambda_{ij})$$

$$F_{y_{ij}} = C_\alpha \frac{\tan(\alpha_{ij})}{1 - \sigma_{x_{ij}}} f(\lambda_{ij})$$

$$f(\lambda_{ij}) = \begin{cases} (2 - \lambda_{ij})\lambda_{ij} & \text{for } \lambda_{ij} < 1 \\ 1 & \text{for } \lambda_{ij} > 1 \end{cases}$$

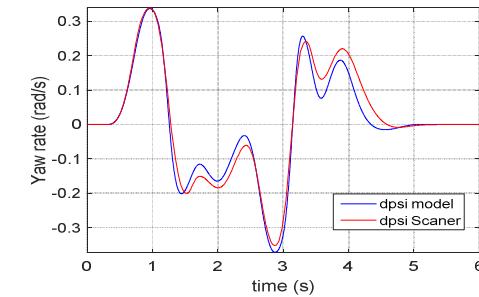
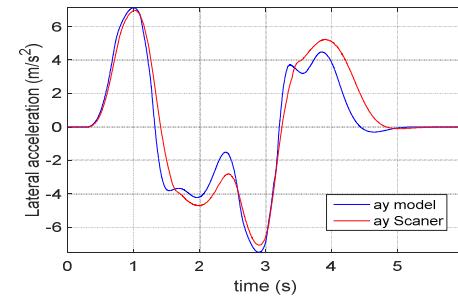
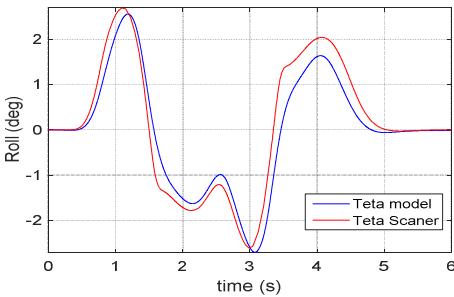
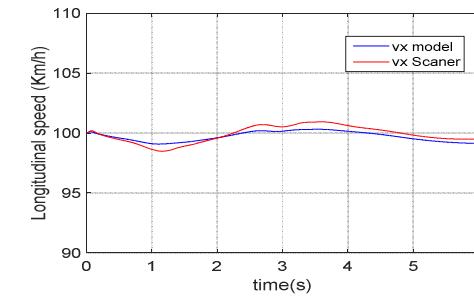
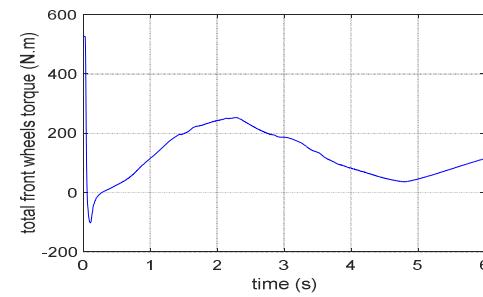
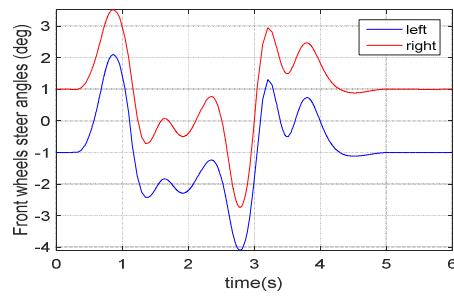
$$\lambda_{ij} = \frac{\mu F_{z_{ij}}(1 - \sigma_{x_{ij}})}{2 \cdot \sqrt{(C_\sigma \sigma_{x_{ij}})^2 + (C_\alpha \tan(\alpha_{ij}))^2}}$$

# Simulation – Renault Megane Parameters

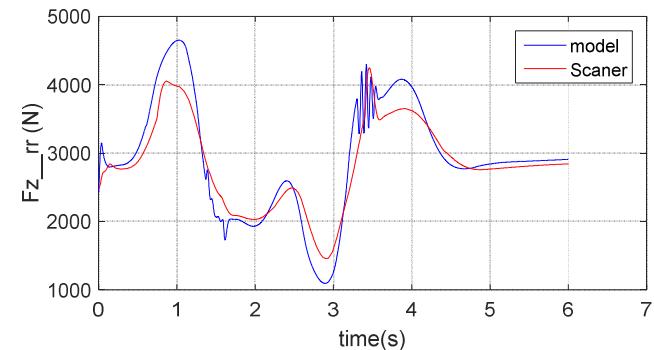
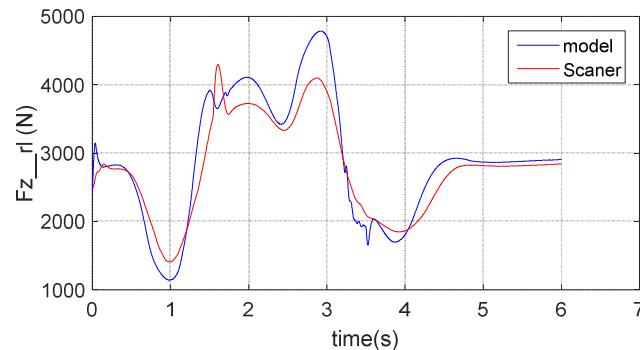
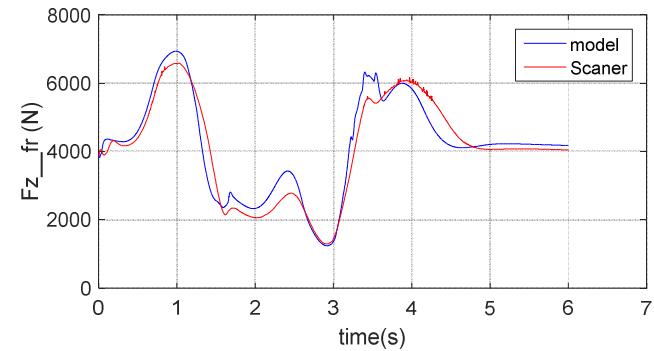
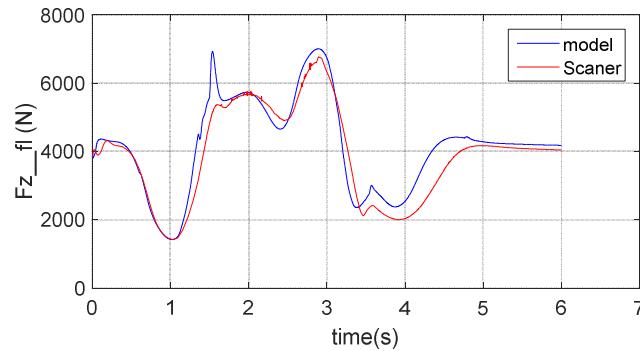
$h=0,58 \text{ m}$

M	1286.4	$t_f = t_r$	0.773
$m_{usij}$	40	$l_f \& l_r$	1 & 1.6
$I_x$	534	$k_{sfl} = k_{sfr}$	22639
$I_y$	1860	$k_{srl} = k_{srr}$	12548
$I_z$	1970	$c_{sij}$	700

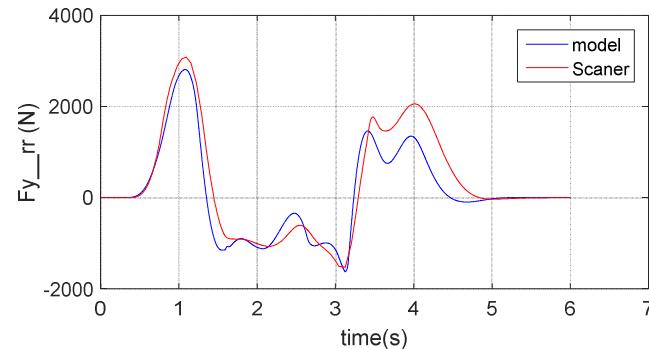
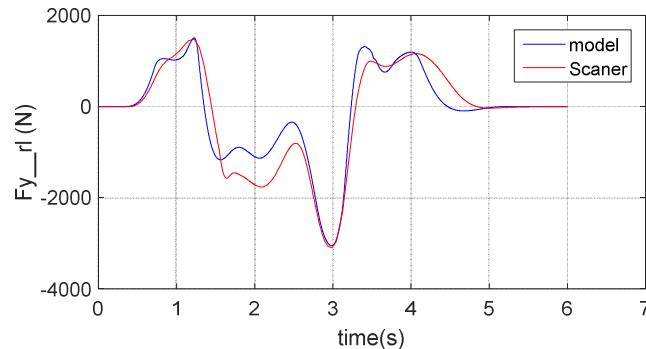
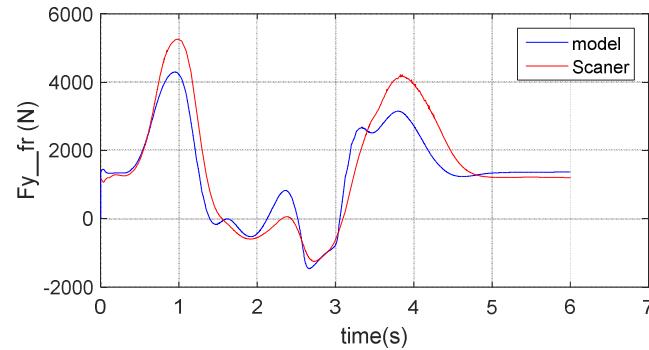
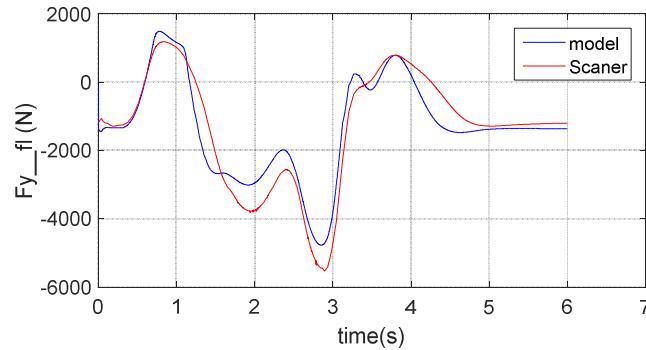
# Model Validation- Scaner Studio



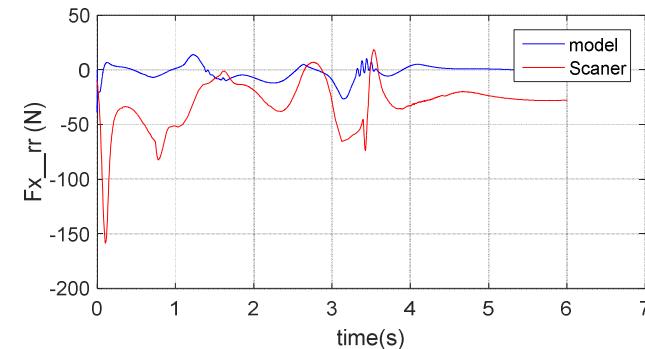
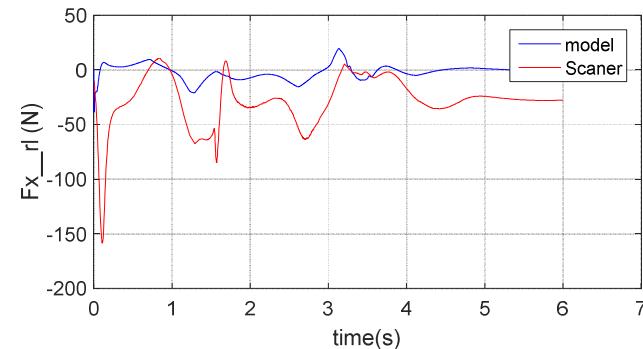
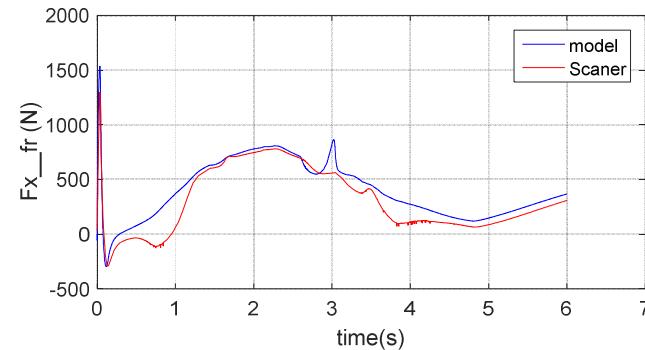
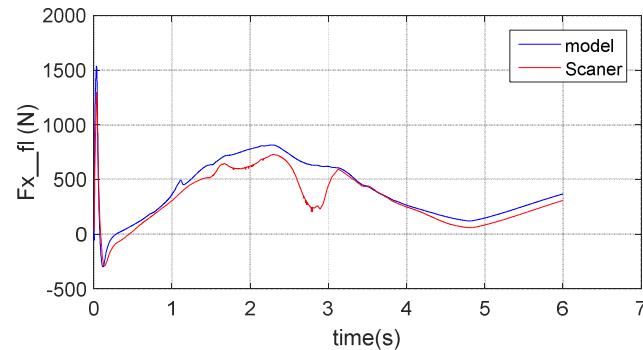
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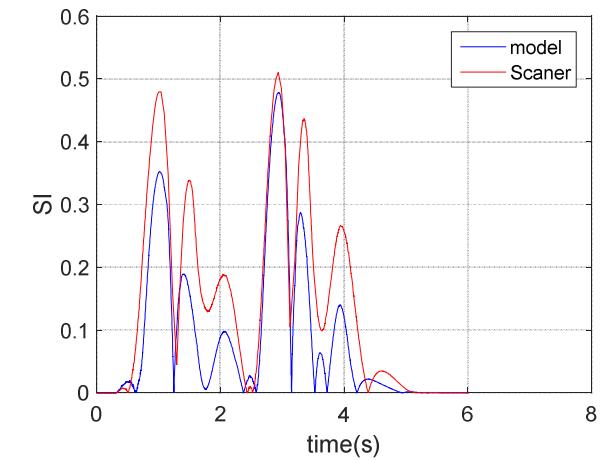
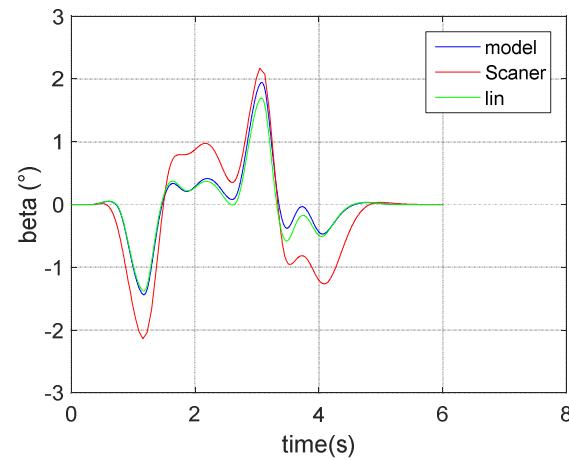
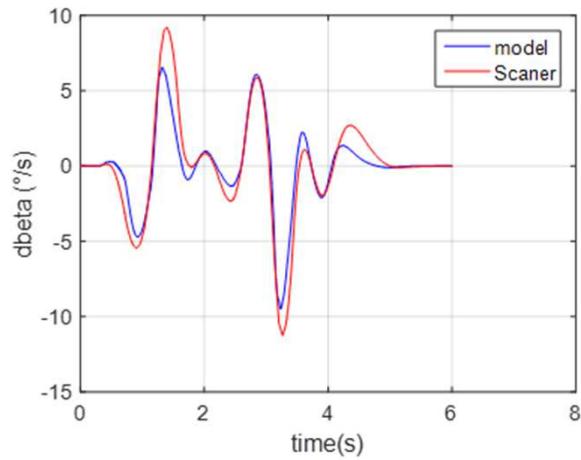
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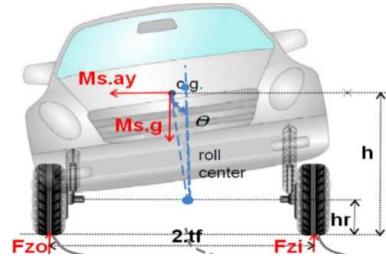
# Model Validation- Scaner Studio



# Model Validation- Scaner Studio



# Active suspensions design for rollover avoidance



- $\theta_{des} = 0$  when  $a_y=0$ ;
- $\theta_{des}$  decreases linearly to attain  $-10^\circ$  (the maximal possible roll angle) when  $a_y$  reaches its maximal safe value  $0.7 * \frac{t_f}{h} \cdot g$ .

$$\ddot{\theta} = \frac{1}{I_x + M_s h_\theta^2} \left( \begin{array}{l} (-F_{sfr} + F_{sfl}) t_f + (-F_{srr} + F_{srl}) t_r \\ + M_s (h_\theta \cos \theta + z) \cdot a_y + M_s (h_\theta \sin \theta + z) \cdot g \end{array} \right)$$

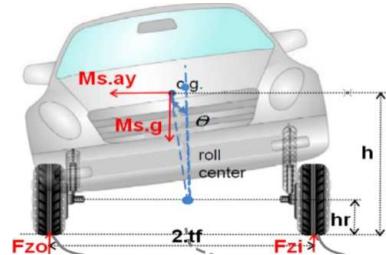
$$F_{sij} = -k_{sij} (z_{sij} - z_{usij}) - c_{sij} (\dot{z}_{sij} - \dot{z}_{usij}) + U_{ij}$$

$$\ddot{\theta} = \frac{1}{I_x + M_s h_\theta^2} \left( \begin{array}{l} \mathcal{M}_\theta + (-F_{fr} + F_{fl}) t_f + (-F_{rr} + F_{rl}) t_r \\ + M_s (h_\theta \cos \theta + z) \cdot a_y + M_s (h_\theta \sin \theta + z) \cdot g \end{array} \right)$$

$$F_{ij} = -k_{sij} (z_{sij} - z_{usij}) - c_{sij} (\dot{z}_{sij} - \dot{z}_{usij})$$

$$\boxed{\theta_{des} = -\frac{10 \cdot \pi / 180}{0.7 * \frac{t_f}{h} \cdot g} a_y}$$

# Active Suspensions controller design



Lyapunov Based controller

$$\ddot{\theta} = \frac{1}{I_x + M_s h_\theta^2} \left( \mathcal{M}_\theta + (-F_{fr} + F_{fl})t_f + (-F_{rr} + F_{rl})t_r + M_s(h_\theta \cos \theta + z).a_y + M_s(h_\theta \sin \theta + z).g \right)$$

$$\begin{aligned} e_\theta &= \theta - \theta_{des}, \\ s_\theta &= \dot{e}_\theta + k_{1\theta} e_\theta + k_{2\theta} \int_0^t e_\theta d\tau, \\ V_\theta &= \frac{1}{2} s_\theta^2, \\ \dot{s}_\theta &= -\alpha_\theta s_\theta, \end{aligned}$$

$$\boxed{\theta_{des} = -\frac{10 \cdot \pi / 180}{0.7 * \frac{t_f}{h} \cdot g} a_y}$$

$$\begin{aligned} \mathcal{M}_\theta &= -(\alpha_\theta + k_{1\theta})(I_x + M_s h_\theta^2)(\dot{\theta} - \dot{\theta}_{des}) - (\alpha_\theta k_{1\theta} + k_{2\theta})(I_x + M_s h_\theta^2)(\theta - \theta_{des}) \\ &\quad - \alpha_\theta k_{2\theta}(I_x + M_s h_\theta^2) \int_0^t (\theta - \theta_{des}) d\tau - (-F_{fr} + F_{fl})t_f - (-F_{rr} + F_{rl})t_r - M_s(h_\theta \cos \theta + z)a_y - M_s(h_\theta \sin \theta + z).g \\ &\quad + (I_x + M_s h_\theta^2)\dot{\theta}_{des}. \end{aligned}$$

# Active Suspensions controller design

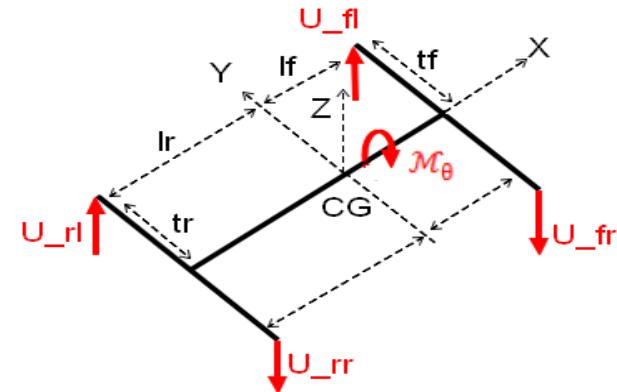
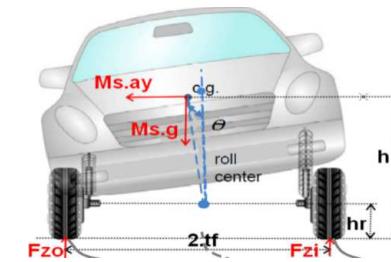
$$\mathcal{M}_\theta = (-U_{fr} + U_{fl})t_f + (-U_{rr} + U_{rl})t_r,$$

$$U_{fl} = 0.5 \frac{\mathcal{M}_\theta}{t_f} \cdot \frac{l_r}{l_f + l_r},$$

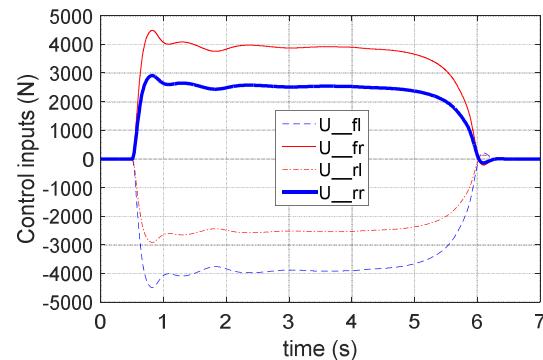
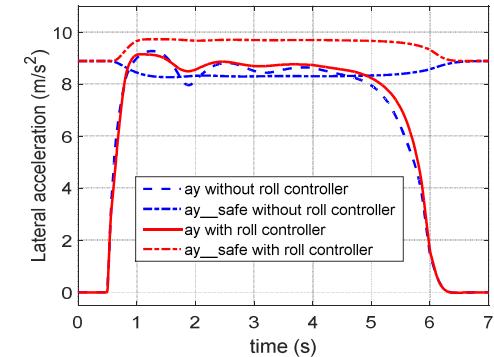
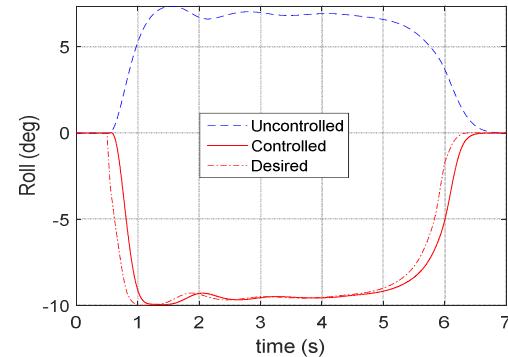
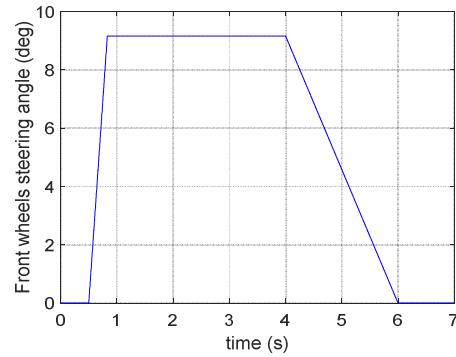
$$U_{fr} = -0.5 \frac{\mathcal{M}_\theta}{t_f} \cdot \frac{l_r}{l_f + l_r},$$

$$U_{rl} = 0.5 \frac{\mathcal{M}_\theta}{t_r} \cdot \frac{l_f}{l_f + l_r},$$

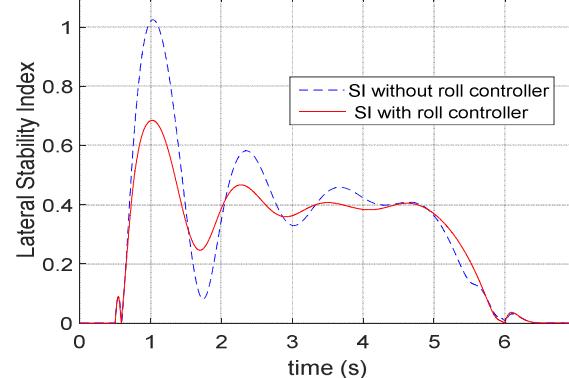
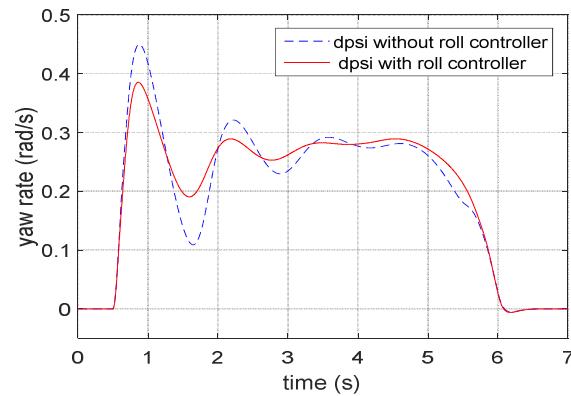
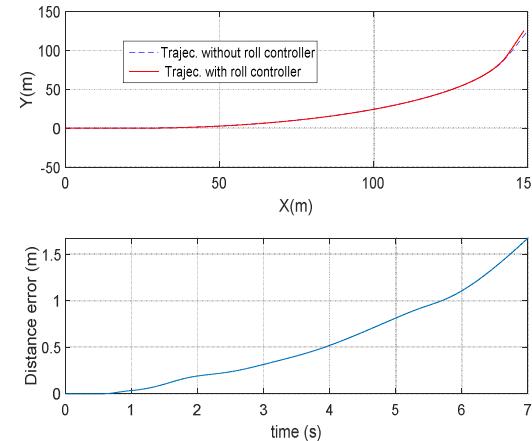
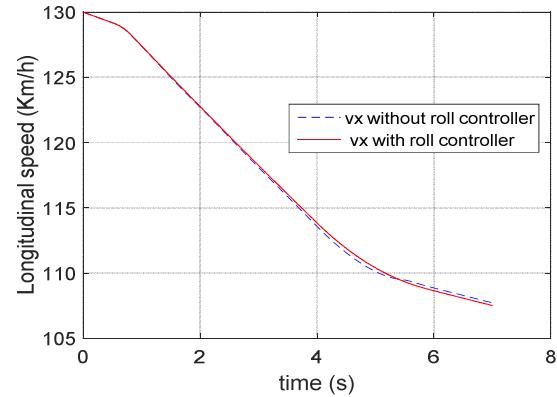
$$U_{rr} = -0.5 \frac{\mathcal{M}_\theta}{t_r} \cdot \frac{l_f}{l_f + l_r}.$$



# Controller validation $V_0 = 130 \text{ Km/h}$



# Controller observations – Side Advantages



## Conclusion

- Develop and Validate a full-vehicle model on Scaner Studio.
- Study of rollover phenomenon and possible solutions.
- Active suspensions control for rollover avoidance.
- Active suspensions advantages on vehicle lateral dynamics.
- Comfort + perturbation isolation (ITSC 2016).

# Perspectives

- Active suspensions for lateral stability
- Active suspensions decision layer (comfort, perturbation isolation, rollover avoidance, lateral stability)
- Global chassis control, a decision layer to coordinate active suspension, differential braking, and active steering.
- Vehicle actuators fault tolerant control.



**Thank you for your  
attention!**